Student Name:	Student ID #
UOSA Statement of Academic	Integrity
On my honor I affirm that I have this exercise.	neither given nor received inappropriate aid in the completion of
Signature:	Date:

Notes Regarding this Examination

- **Open Book(s)** You may consult any printed textbooks in your immediate possession during the course of this examination.
- **Open Notes** You may consult any printed notes in your immediate possession during the course of this examination.
- **No Electronic Devices Permitted** You may not use any electronic devices during the course of this examination, including but not limited to calculators, computers, and cellular phones. All electronic devices in the student's possession must be turned off and placed out of sight (for example, in the student's own pocket or backpack) for the duration of the examination.
- **Violations** Copying another's work, or possession of electronic computing or communication devices in the testing area, is cheating and grounds for penalties in accordance with school policies.

Question 1: Well-Formed Formulas (10 points)

Consider the following well-formed formula: $\neg(p \land q) \rightarrow (p \lor q)$

A. Is it satisfiable? *Justify* your answer.

B. Is it tautologous? *Justify* your answer.

C. Draw its circuit diagram.

Question 2: Well-Formed Formulas (10 points)

Consider the following well-formed formula: $((p \wedge q) \rightarrow r) \rightarrow ((p \rightarrow q) \rightarrow r)$

A. Is it a contradiction? *Justify* your answer.

B. Is it tautologous? *Justify* your answer.

C. Draw its circuit diagram.

Question 3: Natural Deduction (10 points)

Consider the following partial proof of this theorem: $(a \land b) \lor c \vdash (a \lor c) \land (b \lor c)$

Partial proof:

Rewrite the partial proof in the space below, filling in the missing parts (marked with '?' in the proof). If there are any assumptions to be discharged, mark those assumptions and indicate the rule citations that cause those discharges.

Question 4: Natural Deduction (15 points)

Prove the following theorem using natural deduction: $a \rightarrow b, \ b \rightarrow c, \ c \rightarrow d \quad \vdash \quad a \rightarrow d$

If there are any assumptions to be discharged, mark those assumptions and indicate the rule citations that cause those discharges.

Question 5: Natural Deduction (15 points)

Prove the following theorem using natural deduction: $(a \land b) \rightarrow c \vdash a \rightarrow (b \rightarrow c)$

If there are any assumptions to be discharged, mark those assumptions and indicate the rule citations that cause those discharges.

Question 6: Equational Reasoning (20 points)

Prove the following equation using the equations of Boolean algebra:

$$(\neg a \rightarrow b) \rightarrow \neg (c \rightarrow \neg d) = (a \rightarrow (c \land d)) \land (b \rightarrow (c \land d))$$

Question 7: Equational Reasoning (20 points)

Prove the following equation using the equations of Boolean algebra:

$$(b \rightarrow a) \land (\neg b \rightarrow a) = a$$