# AME 3623 Real-Time Embedded Systems <br> Final Exam <br> May 7, 2018 

General instructions:

- Please wait to open this exam booklet until you are told to do so.
- This examination booklet has 14 pages. You also have been issued a bubble sheet.
- Write your name, university ID number and date below, and sign where indicated. Also, write your name and ID number on your bubble sheet, and fill in the bubbles for your ID.
- The exam is closed book, notes and electronic devices. The exception is that you may have one page of personal notes (double sided).
- The exam is worth a total of 274 points (and $20 \%$ of your final grade).
- You have 2 hours to complete the exam. Be a smart test taker: if you get stuck on one problem go on to the next.
- Use your bubble sheet to answer all multiple-choice questions. Make sure that the question number and the bubble row number match when you are answering each question. Use the provided space in this exam booklet to answer the FSM drawing questions.

On my honor, I affirm that I have neither given nor received inappropriate aid in the completion of this exam.
Signature: _ Name:
ID Number: $\quad$ Date:

| Question | Points | Score |
| :---: | :---: | :---: |
| Number Representations and Operations | 45 |  |
| Circuits | 45 |  |
| Circuits and Code | 61 |  |
| Control | 24 |  |
| Interrupt Service Routines | 23 |  |
| Serial Processing | 20 |  |
| Digital-Analog Systems | 16 |  |
| Finite State Machines | 40 |  |
| Total: | 274 |  |

Part I. Number Representations and Operations

1. (5 points) What is the decimal representation of $b$ after the following code is executed?
uint8_t $\mathrm{a}=20$;
uint8_t $\mathrm{b}=14 *(\mathrm{a} / 3)$;
A. 80
B. 84
C. 93
D. 93.3333...
E. Answer not shown
2. (5 points) What is the hexadecimal fixed-point representation of 17.125 using " 12.4 " fixed-point?
A. $0 x 101$
B. $0 \times 102$
C. $0 \times 111$
D. $0 \times 112$
E. Answer not shown
3. (5 points) What is the binary representation for -0x18? Assume a signed, 8-bit integer.
A. 00010010
B. 00011000
C. 11101000
D. 11101110
E. Answer not shown
4. (5 points) What is the decimal value of $c$ after the following code is executed? Assume a " 4.4 " fixed-point representation.
```
uint8_t a = 4;
uint8_t b = 20;
uint8_t c = fixed_point_div(a, b);
```

A. 0
B. 2
C. 3
D. 4
E. Answer not shown
5. (5 points) What is the binary representation of $a$ after the following code is executed?
uint8_t $a=0 \times 7 \mathrm{C}$;
A. 01101010
B. 01101110
C. 01111100
D. 01111110
E. Answer not shown
6. ( 5 points) What is printed by the following code block?

```
int8_t a = 0x92;
int8_t a = Nerial.printf("%d\n", a)
```

A. -146
B. -110
C. 92
D. 146
E. Answer not shown
7. (5 points) What is the minimum value that can be represented with an unsigned, "4.4" fixed-point number?
A. $7 \frac{7}{8}$
B. $7 \frac{15}{16}$
C. $15 \frac{7}{8}$
D. $15 \frac{15}{16}$
E. Answer not shown
8. (5 points) What is the hexadecimal representation of $c$ after the following code is executed?

```
uint8_t a = 0x27;
uint8_t b = 0x26;
uint8_t c = (a ^ 10) & b; // XOR
```

A. $0 \times 24$
B. $0 \times 26$
C. $0 \times 27$
D. $0 \times 28$
E. Answer not shown
9. (5 points) What is the decimal value of $c$ after the following code is executed? Assume a " 12.4 " fixed-point representation.

```
uint16_t a = 0x23;
uint16_t b = 0x13;
uint16_t c = fixed_point_sub(a, b);
```

A. 0 x 0
B. $0 \times 10$
C. $0 \times 100$
D. 0 x 160
E. Answer not shown

Part II. Circuits

Consider the following circuit:


Assume that $R=250 \Omega$ and that $L$ is a logical output.
10. (8 points) If $V_{i n}=7 \mathrm{~V}$, what is $V_{1}$ ?
A. 1 V
B. 2 V
C. $3 V$
D. 4 V
E. Answer not shown
11. (8 points) If $V_{i n}=6.5 V$, what is $L$ ?
A. True
B. False
C. Answer not shown
12. (8 points) If $V_{i n}=1.5 V$, what is $L$ ?
A. True
B. False
C. Answer not shown
13. (5 points) Given the following circuit and $R=200 \Omega, V_{1}=6 \mathrm{~V}$ and $V_{2}=2 \mathrm{~V}$. What is $I$ ?

A. $-30 m A$
B. $-20 m A$
C. -10 mA
D. 10 mA
E. Answer not shown

Consider the following circuit:


Assume that $V_{f}=2 V$ and $R=1000 \Omega$.
14. (8 points) If $V_{2}=4 V, V_{3}=3 V$, what is $V_{1}$ ?
A. 1 V
B. 2 V
C. 3 V
D. 4 V
E. Answer not shown
15. (8 points) If $I_{D}=10 \mathrm{~mA}, V_{3}=0 \mathrm{~V}$, what is $V_{1}$ ?
A. $-2 V$
B. 1 V
C. 2 V
D. 10 V
E. Answer not shown

Page 5

## Part III. Circuits and Code

Consider the following circuit:


Assume $R_{0}=50 \Omega, R_{1}=200 \Omega$ and the maximum voltage output by a microprocessor pin is 5 V .
16. (5 points) What is the correct initialization for $P O R T D \_P D D R$ ?
A. $0 x 03$
B. $0 x 30$
C. $0 x 60$
D. $0 x C 0$
E. Answer not shown
17. (8 points) If $P O R T D_{-} P D O R=0 x 46$, what is $V$ ?
A. 0 V
B. 1 V
C. 4 V
D. 5 V
E. Answer not shown
18. (8 points) If $P O R T D_{-} P D O R=0 x A 8$, what is $V$ ?
A. 0 V
B. 1 V
C. 4 V
D. 5 V
E. Answer not shown
19. (8 points) If $P O R T D_{-} P D O R=0 x 95$, what is $V$ ?
A. 0 V
B. 1 V
C. 4 V
D. 5 V
E. Answer not shown

Consider the following circuit:


Assume that Port C, pins $0 . .3$ are configured as digital output pins. Also assume that the motor can be modeled as a $2 \Omega$ resistor.
20. ( 8 points) When val0 $=0 x 0$ and val $1=0 x 0$, what is the duty cycle of the signal on $C 3$ ?
A. $0 \%$
B. $25 \%$
C. $50 \%$
D. $100 \%$
E. Answer not shown
21. ( 8 points) When val $0=0 x 5$ and val $=0 x 0$, what is the duty cycle that the motor is being driven at?
A. $0 \%$
B. $25 \%$
C. $50 \%$
D. $100 \%$
E. Answer not shown
22. ( 8 points) When val0 $=0 x 3$ and val $1=0 x 0$, what is the average current through the motor?
A. $0 A$
B. $0.625 A$
C. 1.25 A
D. 2.5 A
E. Answer not shown
23. ( 8 points) When val0 $=0 x 0$ and val $1=0 x 5$, what is the average current through the motor?
A. 0 A
B. $0.625 A$
C. $1.25 A$
D. $2.5 A$
E. Answer not shown

## Part IV. Control

Consider the following rotational P-D control law:
$\tau=K_{p}\left(\theta_{d}-\theta\right)+K_{v}\left(\dot{\theta_{d}}-\dot{\theta}\right)$
Assume that positive orientation and torque both refer to the same direction.
24. (6 points) In order to achieve critical damping, what is the sign of $K_{v}$ ?
A. $K_{v}>0$
B. $K_{v}<0$
25. (6 points) The full $K_{p}$ term in the control equation can best be described physically as:
A. a spring
B. a velocity
C. a position
D. friction
E. Answer not shown

Consider the two phase diagrams:



Note: assume the control equations on the previous page and that $\theta_{d}=0$ for all time. Also assume that the initial configuration corresponds to the large, filled dot.
26. (6 points) In phase diagram $\mathbf{b}$, changing the system behavior from trajectory $A$ to trajectory B can be accomplished by which of the following?
A. $K_{p}$ can be decreased or $K_{v}$ can be decreased.
B. $K_{p}$ can be decreased or $K_{v}$ can be increased.
C. $K_{p}$ can be increased or $K_{v}$ can be decreased.
D. $K_{p}$ can be increased or $K_{v}$ can be increased.
E. Answer not shown.
27. (6 points) In phase diagram a, what can be changed in order to improve the performance of the system?
A. $K_{p}$ can be decreased or $K_{v}$ can be decreased.
B. $K_{p}$ can be decreased or $K_{v}$ can be increased.
C. $K_{p}$ can be increased or $K_{v}$ can be decreased.
D. $K_{p}$ can be increased or $K_{v}$ can be increased.
E. Answer not shown.

## Part V. Interrupt Service Routines

Consider the following code:

```
volatile uint8_t d = 100;
void myISR() {
    static uint8_t x = 0;
    + +x;
    if(x== d) { // equal
        GPIOD_PDOR ^= 0x40; // XOR
        x = 0;
    }
}
int setup() {
    // Configure PORTD, bit 6 to be digital I/O
    PORTD_PCR6 = PORT_PCR_MUX (0x1);
    // Configure bit 6 to be an output
    GPIOD_PDDR = 0 x 40;
    // Configure the timer
    Timer1.initialize(100);
    Timer1.attachInterrupt(myISR);
    Timer1.start();
    d = ???
}
loop() {
}
```

28. (6 points) When $d=10$, what is the frequency of the signal at PORT $\mathrm{D}, \operatorname{pin} 6$ ?
A. 10 Hz
B. 100 Hz
C. $1,000 \mathrm{~Hz}$
D. $10,000 \mathrm{~Hz}$
E. Answer not
shown

Solution: 500 Hz
29. (6 points) What is the interrupt frequency?
A. 10 Hz
B. 100 Hz
C. $1,000 \mathrm{~Hz}$
D. $10,000 \mathrm{~Hz}$
E. Answer not shown
30. (6 points) When $d=64$, what is the duty cycle of the signal at PORT D , pin 6 ?
A. $0 \%$
B. $25 \%$
C. $50 \%$
D. $100 \%$
E. Answer not shown
31. (5 points) This is an example of what type of interrupt?
A. Internally-generated
B. Externally-generated

## Part VI. Serial Processing

32. (5 points) True or False: a start bit is used in an asynchronous serial protocol. A. True B. False
33. (15 points) Fill in the implementation of the following function that takes as input a character and returns -1 if the character is a lower case letter, 1 if the character is an upper case letter, 2 if the character is a numerical digit and 0 for all other characters.
$\square$

## Solution:

```
int8_t char_type(char c) {
    if(c>= 'a'&& c<= 'z'){
        return -1;
    }else if(c>= 'A' && c <= 'Z'){
        return 1;
    }else if (c>='0'&& c <= '9') {
        return 2;
    }else{
        return 0;
    }
```


## Part VII. Digital-Analog Systems

34. (8 points) Assume an 8-bit analog-to-digital converter that uses the successive approximation algorithm, and has a range of 0 to 5 volts. If $V_{i n}=3 \mathrm{~V}$ and the first guess by successive approximation is 10000000 , what is the sixth guess?
A. 10011000
B. 10011001
C. 10011010
D. 10011100
E. Answer not shown
35. (8 points) Assume an 4-bit digital-to-analog converter with a range of 0 to 5 volts. What is the voltage that corresponds to the digital value 1001?
A. $9 / 51 \mathrm{~V}$
B. $45 / 63 \mathrm{~V}$
C. $45 / 31 \mathrm{~V}$
D. 3 V
E. Answer not shown

## Part VIII. Finite State Machines

36. (25 points) Consider a light control system for an intersection between a highway and a rural road. The behavior of the light is as follows:
37. By default, the light should be green for the highway (and red for the rural road).
38. The only time that the rural road is given a green light is when a car is detected.
39. Any transition from yellow to red must take 10 seconds.
40. Any transition from red turning on along one direction to green turning on along the orthogonal direction must take 5 seconds.
The events are as follows:

- Timeout(s): $s$ seconds have passed since timer reset. TO(s)
- Car detected from rural road. C
- No Car detected from rural road. NC

The actions are as follows:

- Highway(color): turn highway light to color. HW(c), where c is one of R, Y, G.
- Rural(color): turn rural light to color. $\mathrm{R}(\mathrm{c})$, where c is one of $\mathrm{R}, \mathrm{Y}, \mathrm{G}$.
- Timer reset. TR.

Draw the Finite State Machine that controls these lights.

```
Solution:
```

Consider the following FSM:


This FSM has the following inputs: $\mathrm{x}, \mathrm{a}, \mathrm{b}$, and the following outputs:

- $\mathrm{x}=$ no output
- $0=$ output a zero
- $1=$ output a one

37. (5 points) Suppose the following sequence of inputs is given: $\mathbf{b}, \mathbf{b}$. What is the output?
A. 0
B. 00
C. 1
D. 11
E. Answer not shown
38. (5 points) Suppose the following sequence of inputs is given: $\mathbf{a}, \mathbf{b}, \mathbf{b}$. What is the output?
A. 0
B. 00
C. 1
D. 11
E. Answer not shown
39. (5 points) Suppose the following sequence of inputs is given: $\mathbf{a}, \mathbf{a}, \mathbf{b}, \mathbf{a}, \mathbf{b}, \mathbf{b}, \mathbf{a}$, a. What is the output?
A. 01
B. 000
C. 011
D. 111
E. Answer not shown
