

CFI-Stream: Mining Closed Frequent Itemsets in Data Streams

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ABSTRACT

Mining frequent closed itemsets provides complete and condensed information for non-redundant association rules generation. Extensive studies have been done on mining frequent closed itemsets, but they are mainly intended for traditional transaction databases and thus do not take data stream characteristics into consideration. In this paper, we propose a novel approach for mining closed frequent itemsets over data streams. It computes and maintains closed itemsets online and incrementally, and can output the current closed frequent itemsets in real time based on users' specified thresholds. Experimental results show that our proposed method is both time and space efficient, has good scalability as the number of transactions processed increases and adapts very rapidly to the change in data streams.

Categories and Subject Descriptors

H.2.8 [Database Management]: Database Applications – *Data Mining*.

General Terms

Algorithms, Performance, Experimentation.

Keywords

Data stream, frequent closed itemsets, association rules.

1. INTRODUCTION

Frequent closed itemsets provide complete and condensed information for non-redundant association rules generation. Recently, much research has been done on closed itemsets mining [9, 11-13], but it is mainly for traditional databases where multiple scans are needed, and whenever new transactions arrive, additional scans must be performed on the updated transaction database; therefore, they are not suitable for data stream mining. A data stream is an ordered sequence of transactions that arrives in a timely order. Different from data in traditional static databases, data streams have the following characteristics. First, they are continuous, unbounded, and usually come with high speed. Second, the volume of data streams is large and usually with an open end. Third, the data distribution in streams usually changes with time.

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As the number of applications on mining data streams grows rapidly, such as web transactions, telephone records, and network flows, much research on how to get frequent patterns in a data stream environment has been conducted. In [2, 7, 10], the authors propose algorithms to find frequent itemsets over the entire history of data streams. In [3, 5, 8], different sliding window models are used to find recently frequent itemsets in data streams. These algorithms focus on mining frequent itemsets, instead of closed frequent itemsets, with one scan over entire data streams.

In [4], Chi et al propose the Moment algorithm to mine closed frequent itemsets over a data stream sliding window. The algorithm maintains a dynamically selected set of itemsets which includes four types of nodes: infrequent gateway nodes, unpromising gateway nodes, intermediate nodes, and closed nodes. For each node, the itemset itself, node type, support and sum of the ids of the transactions in which the itemset occurs (tid_sum) are stored. These selected itemsets form a boundary between closed frequent itemsets and the rest of the itemsets. When a new transaction arrives, it checks the closed frequent itemsets stored in a hash table with its support and tid_sum information to decide its node type according to the node properties and incrementally updates the associated nodes' information. Moment judges the closed itemsets indirectly through node property checking and excludes them from the other three types of boundary nodes stored in the data structure. It stores much more information other than the current closed frequent itemsets, which consumes much memory, especially when the support threshold is low. Furthermore, the exploration and node type checking are time consuming.

In this study, we propose an algorithm, called CFI-Stream, to directly compute closed itemsets online and incrementally without the help of any support information. Nothing other than closed itemsets is maintained in our derived data structure. When a new transaction arrives, it performs the closure checking on the fly; only associated closed itemsets and their support information is incrementally updated. This achieves both time and space efficiency, especially when a dataset contains highly correlated transactions. The current closed frequent itemsets can be output in real time based on any user's specified thresholds. We then conduct simulation experiments using synthetic data sets to evaluate the performance of our proposed algorithm.

The rest of this paper is organized as follows. Section 2 formally defines the concept of closed itemsets and describes the notations to be used throughout the paper. Section 3 presents our proposed CFI-Stream algorithm. The performance evaluation is depicted in Section 4. Finally, Section 5 concludes the paper.

2. PRELIMINARY CONCEPTS

Let $I = \{i_1, i_2, \dots, i_n\}$ be a set of n elements, called items. A subset $X \subseteq I$ is called an itemset. A k -subset is called a k -itemset. Each transaction t is a set of items in I . Given a set of transactions T , the support of an itemset X is the percentage of transactions that contain X .

Let T and X be subsets of all the transactions and items appearing in a data stream D , respectively. The concept of a closed itemset is based on the two following functions, f and g : $f(T) = \{i \in I \mid \forall t \in T, i \in t\}$ and $g(X) = \{t \in D \mid \forall i \in X, i \in t\}$. Function f returns the set of itemsets included in all transactions belonging to T , while function g returns the set of transactions containing a given itemset X .

Definition 1 An itemset X is said to be closed if and only if $C(X) = f(g(X)) = f \bullet g(X) = X$ where the composite function $C = f \bullet g$ is called a Galois operator or a closure operator.

From the above discussion, we can see that a closed itemset X is an itemset whose closure $C(X)$ is equal to itself ($C(X) = X$). The closure checking is to check the closure of an itemset X to see whether or not it is equal to itself, i.e. whether or not it is a closed itemset.

3. THE CFI-STREAM ALGORITHM

In this section, we present our proposed CFI-Stream algorithm and in-memory data structure, called Direct Update (DIU) tree, to perform the closure checking online over a data stream sliding window. We first give an overview of CFI-Stream. Then, we discuss the conditions that we need to check for closed itemsets and how we check for them when performing addition and deletion operations on the DIU tree. Based on this, we develop an online algorithm to discover and incrementally update closed itemsets.

3.1 Algorithm Overview

When a transaction arrives or leaves the current data stream sliding window, the algorithm checks each itemset in the transaction on the fly and updates the associated closed itemsets' supports. Current closed itemsets are maintained and updated in real time in the DIU tree. The closed frequent itemsets can be output at any time at users' specified thresholds by browsing the DIU tree.

We use a lexicographical ordered DIU tree to maintain the current closed itemsets. Each node in the DIU tree represents a closed itemset. There are k levels in the DIU tree, each level i stores the closed i -itemsets, where k is the maximum length of the current closed itemsets. Each node in the DIU tree stores a closed itemset, its current support information, and the links to its immediate parent and children nodes. Figure 1 illustrates the DIU tree after the first four transactions arrive. The support of each node is labeled in the upper right corner of the node itself. The figure shows that currently there are 4 closed itemsets, C , AB , CD , and ABC in the DIU tree, and their associated supports are 3, 1, and 2.

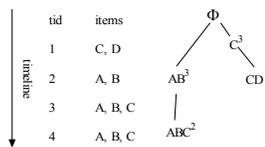


Figure 1. The lexicographical ordered direct update tree

Different from previous closure checking techniques which require multiple scans over data [9, 11-13], our proposed method performs the closure checking on the fly with only one scan over data streams. It updates only the supports of the associated closed itemsets in the DIU tree online, which reduces the computation time and provides real time updated results. Our algorithm is an incremental algorithm where we check for closed itemsets and update their associated supports based on the previous mining results. This is more efficient as compared with mining approaches that rescan and regenerate all closed itemsets when a new transaction arrives.

Compared with other data stream mining techniques [4, 8, 10], we store only the information of current closed itemsets in the DIU tree, which is a compact and complete representation of all itemsets and their support information. The current closed frequent itemsets can be output in real time based on users' specified thresholds by browsing the DIU tree. Also, our algorithm handles the concept-drifting problem in data streams by storing all current closed itemsets in the DIU tree from which all itemsets and their support information can be incrementally updated. We discuss the update of the DIU tree and the closure checking procedure for addition and deletion operations in Sections 3.2 and 3.3.

3.2 Add a Transaction to the DIU Tree

In this subsection, we discuss the update and maintenance of the DIU tree when a new transaction arrives and its closure check.

3.2.1 Conditions to Check for Closed Itemsets

First, we identify and prove the following conditions in which we need to check whether an itemset is closed or not when a new transaction t arrives in the current sliding window. Condition 1: when the newly arrived transaction t is in the original transaction set, if the largest itemset X it contains is not currently in the DIU tree, we need to check for all X 's subsets Y , which are in the original transaction set to see whether they are closed or not. Condition 2: when the newly arrived transaction t is not in the original transaction set, for each its subset Y , if Y is in the original transaction set, we need to check whether it is closed or not. Below we prove why we only need to check for closed itemsets in the above two conditions. We will use the Lemma 1 and Corollary 1 in our following proofs. The proof of Lemma 1 is given in [9]. Corollary 1 is derived from Lemma 1.

Lemma 1 Given an itemset X and an item $i \in I$, $g(X) \subseteq g(i) \Leftrightarrow i \in C(X)$.

Corollary 1 Assume $C_T(X)$ is X 's closure within transaction set T . If $C_T(X) = X$ and $Y \subset X$ and $C_T(Y) \supset Y$, given an item i , where $i \in C_T(Y)$, $i \notin Y$, then we have $i \in X$ and $C_T(Y) \subseteq X$.

When a new transaction t in the data stream arrives, either t is or is not included in the original transaction set. Below, we discuss the update and maintenance rules under these two conditions. In the following proof, we assume X and Y are itemsets, T_1 is the original set of transactions, T_2 is the set of transactions after t arrives, $C_{T_1}(X)$ is X 's closure in transaction set T_1 , and $C_{T_2}(Y)$ is Y 's closure in transaction set T_2 .

Case 1: When t is in the original transaction set T_1

For any new coming transaction t with the largest itemset X that already exists in the original transaction set T_1 , we have $g_{T_1}(X) \neq \phi$. When $g_{T_1}(X) \neq \phi$, for any itemset Y , $g_{T_1}(Y) = \phi$. If $Y \subset X \Rightarrow g_{T_1}(Y) \supset g_{T_1}(X) \neq \phi$. This is a contradiction with $g_{T_1}(Y) = \phi$. Therefore this condition does not happen. If $Y \not\subset X \Rightarrow g_{T_2}(Y) =$

$g_{T1}(Y) = \phi$. Thus, we do not need to discuss cases when $g_{T1}(Y) = \phi$. When $g_{T1}(X) \neq \phi$ and $g_{T1}(Y) \neq \phi$, we examine cases according to the following conditions: $Y \not\subseteq X$ and $Y \subseteq X$.

Case 1.A: When Y is a subset of X

When Y is a subset of X, $Y \subseteq X$, we divide it into two sub conditions to analyze: X is or is not in the DIU tree.

Case 1.A.1: When X is in the DIU Tree

When X is in the DIU tree, it is a closed itemset, therefore $C_{T1}(X) = X$. We have the following Lemmas 2 and 3. From these two lemmas, we show that if a closed itemset X which already exists in the DIU tree arrives, for any itemset Y, $Y \subseteq X$, if Y is originally closed, it will remain closed; if Y is originally unclosed, Y will remain unclosed, and we only need to update Y's support. Therefore, for most of the existing closed itemsets, we do not need to update the DIU tree structure; we simply update their supports, which consume a small amount of time.

Lemma 2 Given $T2 = T1 \cup \{X\}$, if $C_{T1}(X) = X$ and $Y \subseteq X$ and $C_{T1}(Y) = Y$, then we have $C_{T2}(Y) = Y$.

Lemma 3 Given $T2 = T1 \cup \{X\}$, if $C_{T1}(X) = X$ and $Y \subset X$ and $C_{T1}(Y) \supset Y$, then we have $C_{T2}(Y) \supset Y$.

Case 1.A.2: When X is not in the DIU Tree

When X is not in the DIU tree, it is not a closed itemset, therefore $C_{T1}(X) \supset X$. Similarly, we have the following Lemmas 4 and 5. From Lemma 4, we show that if a new closed itemset which is not originally in the DIU tree arrives and if its subsets are already in the DIU tree, they will remain closed, and thus we simply need to update their supports. From Lemma 5, we show that if a new closed itemset which is not originally in the DIU tree arrives, then we need to add it as a new closed itemset to the DIU tree.

Lemma 4 Given $T2 = T1 \cup \{X\}$, if $C_{T1}(X) \supset X$ and $Y \subset X$ and $C_{T1}(Y) = Y$, then we have $C_{T2}(Y) = Y$.

Lemma 5 Given $T2 = T1 \cup \{X\}$, if $C_{T1}(X) \supset X$ and $Y = X$, then we have $C_{T2}(Y) = Y = X$.

Case 1.B: When Y is not a subset of X

When Y is not a subset of X, $Y \not\subseteq X$, we have the following Lemma 6. In Lemma 6, we show that if Y is not a subset of X, Y's closure does not change. That is to say that if Y is an unclosed itemset before X arrives, then Y will remain unclosed after X arrives; and, if Y is a closed itemset before X arrives, then Y will remain closed after X arrives. Thus, the DIU tree structure does not need to be updated, and we only need to update Y's support.

Lemma 6 Given $T2 = T1 \cup \{X\}$, if $Y \not\subseteq X$, then we have $C_{T2}(Y) = C_{T1}(Y)$.

Case 2: When t is not in the original transaction set T1

For any new coming transaction t with the largest itemset X that has not already appeared in the original transaction set T1, we have $g_{T1}(X) = \phi$. We discuss two sub cases according to the following conditions: $Y \not\subseteq X$ and $Y \subseteq X$.

Case 2.A: When Y is a subset of X

When Y is a subset of X, $Y \subseteq X$, we divide it into two sub conditions to discuss: Y exists in the original transaction set T1 or Y does not exist in the original transaction set T1.

Case 2.A.1: When Y is in the original transaction set T1

When Y is already in the original transaction set T1, then $g_{T1}(Y) \neq \phi$. Because $Y \subseteq X$, we have $g_{T2}(Y) = g_{T1}(Y) \cup \{X\}$. Therefore, $C_{T2}(Y) = C_{T1}(Y) \cap \{X\}$. We will perform the closure checking to decide Y's closure, which will be discussed in Section 3.2.2.

Case 2.A.2: When Y is not in the original transaction set T1

When Y does not exist in the original transaction set T1, then $g_{T1}(Y) = \phi$. We have the following Lemma 7. In this lemma, we prove that when Y is a subset of X, if $Y = X$, then Y is a closed itemset in transaction set T2; and if $Y \subset X$, then Y is not a closed itemset in transaction set T2.

Lemma 7 Given $T2 = T1 \cup \{X\}$, if $Y = X$, then we have $C_{T2}(Y) = Y$; if $Y \subset X$, then we have $C_{T2}(Y) \subset Y$.

Case 2.B: When Y is not a subset of X

When Y is not a subset of X, $Y \not\subseteq X$, we divide it into two sub conditions to discuss: Y is in the original transaction set T1 or Y is not in the original transaction set T1.

Case 2.B.1: When Y is in the original transaction set T1

If Y is already in the original transaction set T1, then $g_{T1}(Y) \neq \phi$. We have the following Lemma 8. Similar to Lemma 6, in this lemma we prove that when Y is not a subset of X, Y's closure does not change in transaction set T2.

Lemma 8 Given $T2 = T1 \cup \{X\}$, if $Y \not\subseteq X$, then $C_{T2}(Y) = C_{T1}(Y)$.

Case 2.B.2: When Y is in the original transaction set T1

If Y is not in the original transaction set, then $g_{T1}(Y) = \phi$. If $Y \subset X$, we have $g_{T2}(Y) = g_{T1}(Y) = \phi$, which is meaningless to discuss.

From the above proofs, we can see that when a new transaction arrives, for most cases, the DIU tree structure does not change and we only need to update the associated itemsets' supports, which thus reduces the processing costs. There are only two cases that we need to perform the closure check: 1) when $g_{T1}(X) \neq \phi$, $g_{T1}(Y) \neq \phi$, $C_{T1}(X) \supset X$, and $Y \subset X$; and 2) when $g_{T1}(X) = \phi$, $g_{T1}(Y) \neq \phi$, and $Y \subseteq X$. We will discuss how to check for closed itemsets in the following section.

3.2.2 Closure Checking for Addition

The CFI-Stream algorithm checks whether an itemset is closed or not on the fly and incrementally with one scan of data streams. Below, we discuss the checking procedure when performing the addition operation on the DIU tree. In the following Theorem 1, we show that for any coming unclosed itemset Y, we can always find one and only one closed itemset in the DIU tree equal to Y's closure, such that $X_c = C(Y)$.

Theorem 1 For any itemset Y, if $C(Y) \supset Y$ and $g(Y) \neq \phi$, then we can always find one and only one closed itemset $X_c \in C$, where C is a set of existing closed itemsets that satisfies $C(Y) = X_c$, where $Y \subset X_c$.

From Theorem 1, we know that for any itemset Y, $C(Y) \supset Y$, we can find X_{c0} with a minimum number of items in it and $X_{c0} \supset Y$. For any other $X_{c1} \supset Y$, from the above discussion we know that $g(X_{c0}) \supset g(X_{c1})$. Because $Y \subset X_{c0}$, then $g(Y) \supseteq g(X_{c0}) \supset g(X_{c1})$. To find $X_c \subseteq C(Y)$, we have $g(X_c) = g(Y)$; only X_{c0} will fulfill this requirement. In this way, $C(Y)$ can be found in the original transaction set T1. Below, we show how we use this $C(Y)$ to check if Y is a closed itemset in transaction set T2 after X arrives.

Corollary 2 Given $T2 = T1 \cup \{X\}$, if $C_{T1}(X) \supset X$ and $g_{T1}(Y) \neq \phi$, $Y \subseteq X$, $C_{T1}(Y) \supset Y$, $(C_{T1}(Y)/Y) \cap X = \phi$, then we have $C_{T2}(Y) = Y$.

From Corollary 2, we derive a way to check whether Y is closed in transaction T2 or not. If $(C_{T1}(Y)/Y) \cap \{X\} = \phi$, then Y is a closed itemset in T2. We use this condition to perform the closed itemset checking on the fly when a new transaction in the data streams arrives.

3.3 Delete a Transaction in DIU Tree

In this subsection, we discuss the update and maintenance of the DIU tree for the deletion operation, which occurs when a transaction leaves the sliding window and its closure check.

3.3.1 Conditions to Check for Closed Itemsets

First, we identify and prove the following condition in which we need to check whether an itemset is closed or not when an old transaction leaves the current sliding window: When the number of the transactions with same itemset of X is equal to zero, if Y is a subset of X , and Y is a closed itemset in the original transaction set, we need to check whether Y is currently closed or not. Below, we prove why we only need to check for closed itemsets in the above condition.

When a transaction t , containing a set of items X , is deleted from the current sliding window, the number of transactions with the same itemsets of X is either greater than or equal to zero. Below, we discuss the update and maintenance rules under these two conditions.

In the following proof, we assume X and Y are itemsets, T_1 is the original set of transactions, T_2 is the set of transactions after itemset X leaves, $C_{T_1}(X)$ is X 's closure within transaction set T_1 , and $C_{T_2}(Y)$ is Y 's closure under transaction set T_2 .

Case 1: When the number of the transactions with the same itemset X is greater than zero

When the number of transactions with the same itemset X is greater than zero, we have the following Lemma 9. From this lemma, we know that Y 's closure does not change when the number of transactions with the same itemset X is greater than zero. That is to say that if Y is an unclosed itemset before X leaves, Y will remain unclosed after X leaves; and if Y is a closed itemset before X leaves, Y will remain closed after X leaves.

Lemma 9 Given $T_2 = T_1 \setminus \{X\}$, $\{X\} \subset T_2$, we have $C_{T_2}(Y) = C_{T_1}(Y)$.

Case 2: When the number of transactions with the same itemset X is equal to zero

When the number of transactions with same itemset of X is equal to zero, $\{X\} \not\subset T_2$, we discuss according to the following two sub conditions: Y is not a subset of X and Y is a subset of X .

Case 2.A: When Y is not a subset of X

If Y is not a subset of X , we have the following Lemma 10. In this lemma, we prove that when $\{X\}$ no longer exists in transaction set T_2 , Y is not a subset of X and Y 's closure does not change in transaction set T_2 .

Lemma 10 Given $T_2 = T_1 \setminus \{X\}$, if $\{X\} \not\subset T_2$, $Y \not\subset X$, $Y \neq X$, then $C_{T_2}(Y) = C_{T_1}(Y)$.

Case 2.B: When Y is a subset of X

If Y is a subset of X , we discuss according to the following sub conditions: Y is a closed itemset in transaction set T_1 and Y is not a closed itemset in transaction set T_1 .

Case 2.B.1: When Y is a closed itemset

When Y is a closed itemset in the transaction set T_1 , that is to say when $Y \subseteq X$, $C_{T_1}(Y) = Y$, we need to perform the closure check, which we will discuss further in Section 3.3.2.

Case 2.B.2: When Y is not a closed itemset

When Y is not a closed itemset in transaction set T_1 , we have the following Lemma 11. In this lemma, we prove that when Y is a subset of X , Y is not a closed itemset in transaction set T_2 .

Lemma 11 Given $T_2 = T_1 \setminus \{X\}$, if $Y \subset X$, $C_{T_1}(Y) \subset Y$, then $C_{T_2}(Y) \subset Y$.

From the above discussion, we can see that when an old transaction leaves the current sliding window, for most cases, the DIU tree structure does not change and we need to update only the associated supports, which thus reduces the update costs. There is only one case in which we need to perform the closure check: when $\{X\} \not\subset T_2$, $Y \subseteq X$, and $C_{T_1}(Y) = Y$. We will discuss how to check for closed itemsets in the following section.

3.3.2 Closure Checking for Deletion

The CFI-Stream algorithm checks whether an itemset is closed or not on the fly and incrementally updates the DIU tree based on the previous mining results with one scan of data streams. Below, we discuss the checking procedure for the deletion operation. In the following Theorem 2, we show that for any itemset Y , if $Y \subseteq X$, $C_{T_1}(Y) = Y$, $\{X\} \notin T_2$, then we can always find $C_{T_2}(Y)$ in the original closed itemsets.

Theorem 2 For any itemset Y , if $Y \subseteq X$, $C_{T_1}(Y) = Y$, $\{X\} \notin T_2$, then $C_{T_2}(Y) \in C_{T_1}$. That is to say, we can always find $C_{T_2}(Y)$ in C_{T_1} .

In the following Lemma 12, we prove that when Y is a subset of X , $\{Y\} \in T_2$. Y is a closed itemset in transaction set T_2 .

Lemma 12 For any itemset Y , if $Y \subset X$, $\{Y\} \in T_2$, we have $C_{T_2}(Y) = Y$.

From the above discussion, we can see that in the condition that we need to perform the closure checking for the deletion operation, if $\{Y\} \in T_2$, the Y is closed in the new transaction set T_2 . Below we show how we perform the closure check when $\{Y\} \notin T_2$, and to see if Y is a closed itemset in transaction set T_2 after X leaves.

Corollary 3 If $Y \subseteq X$, $\{Y\} \notin T_2$, for all $u_1, u_2, \dots, u_i, \dots, u_n$ which satisfies $C_{T_2}(u_i) = u_i$, $Y \subset u_i$, and $C_{T_2}(Y) = u_1 \cap u_2 \cap \dots \cap u_i \cap \dots \cap u_n$.

From Corollary 3, we derive a way to check Y 's closure: if $C_{T_2}(Y) = u_1 \cap u_2 \cap \dots \cap u_i \cap \dots \cap u_n = Y$, then Y is a closed itemset. We use this rule to perform the closure checking in the CFI-Stream algorithm on the fly when old itemsets leave the current sliding window.

3.4 The Algorithm

Based on our discussions in Sections 3.2 and 3.3, we derive an algorithm to perform online checking for closed itemsets over data streams. The CIF-Stream algorithm performs an addition operation when a new transaction arrives and a deletion operation when an old transaction leaves the current sliding window. By performing the addition and deletion operations, the CFI-Stream algorithm checks each itemset in the transaction on the fly and updates the associated closed itemsets' supports. Current closed itemsets are maintained and updated in real time in the DIU tree. The closed frequent itemsets can be output any time at the user's request by traversing the DIU tree.

Algorithm 1 illustrates the addition procedure when an itemset X arrives. It first checks if X is in the current closed itemsets set C . If X is in C , it updates X 's support, and for all X 's subsets Y belonging to C , it updates Y 's supports (lines 3 to 8). Otherwise, if X is not in C and X has been included by at least one transaction in the original transaction set, it checks whether it is a closed itemset for itself and all its subsets (lines 9 to 36); and it updates the associated supports for all the closed itemsets (lines

37 to 40). If X is a newly arrived closed itemset and does not exist in the DIU tree, the algorithm adds it as a new node to the DIU tree (lines 27 to 31). Otherwise, if X is the added transaction itself, it adds X into the closed itemset (lines 10-15); if X is the subset of added transaction, a closure checking is performed (lines 16-24). In the following algorithm description, X and Y represent itemsets, X_s and Y_s represent X 's support and Y 's support, $Len(X)$ represents the length of the itemset X , which is the number of items in an itemset X , C represents the original closed itemsets in the DIU tree, and C_{new} represents new closed itemsets in the DIU tree after itemset X arrives.

Algorithm 1 CFI-Stream – Addition

```

1:  X_close = true; C_new =  $\phi$ ;
2:  procedure Add(X, C, C_new)
3:    if (X  $\in$  C)
4:      for all (Y  $\subseteq$  X and Y  $\in$  C)
5:         $Y_s \leftarrow$  support(Y, C) + 1;
6:      end for
7:      if (X_close = true) return;
8:    else
9:      if (support(X, C) > 0)
10:       if (C_new =  $\phi$ )
11:          $X_0 \leftarrow$  X;
12:         C_new  $\leftarrow$  X;
13:         X_close = false;
14:          $X_s \leftarrow$  support(X, C) + 1;
15:       else
16:          $X_c = \phi$ ;
17:         for all (K  $\supset$  X and K  $\in$  C)
18:           if (len(K) < len(M)) then M=K;
19:         end for
20:          $X_c \leftarrow$  M;
21:         if ((Xc/X)  $\cap$  X0 =  $\phi$  and Xc  $\neq$   $\phi$ )
22:           C_new  $\leftarrow$  C_new  $\cup$  X;
23:            $X_s \leftarrow$  support(X, C) + 1;
24:         end if
25:       end if
26:     else
27:       if (C_new =  $\phi$ ) then
28:          $X_0 \leftarrow$  X;
29:         C_new  $\leftarrow$  X;
30:          $X_s = 1$ ;
31:       end if
32:     end if
33:   end if
34:   for all (m  $\subset$  X and Len(m) = Len(X)-1)
35:     call Add(m, C, C_new);
36:   end for
37:   if (X = X0)
38:     C  $\leftarrow$  C  $\cup$  C_new;
39:     support(X, C) = Xs;
40:   end if
41: end procedure

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Algorithm 2 illustrates the procedure to perform the deletion operation when an itemset X leaves the current sliding window. CFI-Stream first checks if X is in the current closed itemsets set C and its count is greater or equal to two; if so, it updates X 's support and X 's subsets' support belonging to C (lines 3 to 6). Otherwise, it checks the itemset X and all its subsets which are in

the current closed itemset C to see whether they are still closed itemsets (lines 8 to 26) and updates the support for all its subsets that are in the current closed itemsets (lines 28 to 29). If the subset Y exists in transaction, Y should keep closed (lines 11-13). Otherwise a closure check for the subset Y is performed (lines 14-22). In the following figure, $C_{obsolete}$ represents the itemsets that are no longer closed after transaction $\{X\}$ leaves.

Algorithm 2 CFI-Stream – Deletion

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1:  C_obsolete =  $\phi$ ;
2:  procedure Delete(X, C, C_obsolete)
3:    if (count(X)  $\geq$  2) then
4:      for all (Y  $\subseteq$  X and Y  $\in$  C)
5:         $Y_s \leftarrow$  support(Y, C) - 1;
6:      end for
7:    else
8:      length = Len(X);
9:      for all (len  $\geq$  1)
10:       for all (Y  $\subseteq$  X and Y  $\in$  C and Len(Y) = length)
11:         if (count(Y)  $\geq$  2) then
12:            $Y_s \leftarrow$  support(Y, C) - 1;
13:         else
14:           M = I;
15:           for all (U  $\supset$  Y and U  $\in$  C)
16:             M = M  $\cap$  U;
17:           end for
18:           if (M = Y) then
19:              $Y_s \leftarrow$  support(Y, C) - 1;
20:           else
21:             C_obsolete = C_obsolete  $\cup$  Y;
22:           end if
23:         end if
24:       end for
25:       length = length-1;
26:     end for
27:   end if
28:   C  $\leftarrow$  C  $\setminus$  C_obsolete
29:   support(Y, C) = Ys;
30: end procedure

```

4. PERFORMANCE EVALUATION

We compare our algorithm with Moment [4], which is the state-of-the-art algorithm to mine closed itemsets in data streams. For performance evaluation, the synthetic datasets T10.I6.D100K and T5.I4.D100K-AB are used. Each dataset is generated by the same method as described in [1], where the three numbers of each dataset denote the average transaction size (T), the average maximal potential frequent itemset size (I) and the total number of transactions (D), respectively. In all experiments, the transactions of each dataset are looked up one by one in sequence to simulate the environment of an online data stream.

Figure 2 shows the average processing time for Moment and CFI-Stream over the 100 sliding windows under different minimum supports for the dataset T10.I6.D100K. As the minimum support decreases, the running time for Moment increases, since the number of closed frequent itemsets and the boundary nodes increases. For CFI-Stream, the running time is independent of the support information since it discovers and maintains all closed itemsets in the DIU tree. As the number of closed itemsets that exists in the DIU tree increases, they do not need to be reprocessed; only their supports need to be updated

incrementally, therefore less processing time is needed per transaction. Also we can see from Figure 2 that CFI-Stream runs much faster than Moment when the support threshold is relatively low, because the number of boundary nodes stored in the data structure of Moment increases when the support threshold drops; as the number of nodes to be processed and checked for node property increase, execution time increases. When the support threshold is relatively high, these two algorithms have comparable running time. Moment runs a little faster than CFI-Stream as the threshold increases. This is because as the threshold creases, the number of the boundary nodes in Moment decreases, while CFI-Stream processes the same number of all the closed itemsets independent of support information. This is especially beneficial when users have different specified support thresholds in their online queries.

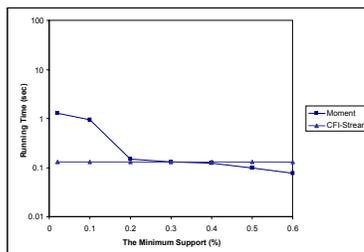


Figure 2. Runtime performance (T10.I6.D100K)

Figure 3 shows the memory usage in terms of the maximum number of itemsets of Moment and CFI-Stream for the dataset T10.I6.D100K. The memory usage for Moment increases when the minimum support decreases. This is because the number of itemsets it keeps track of increases. The memory usage remains almost the same when the support changes in CFI-Stream. This is because CFI-Stream stores all closed itemsets in the DIU tree independently of the support information. The overall memory usage is proportional to the number of closed itemsets in the dataset. Also we can see from the figure that CFI-Stream consumes much less memory space than Moment when the support threshold is low, because when the user defined support threshold is small, the number of nodes it maintains in the memory increases dramatically, which includes all the infrequent gateway nodes, unpromising gateway nodes, intermediate nodes, and closed nodes. As the support threshold increases, the memory usage of Moment drops. These two algorithms consume almost the same amount of memory space. Moment takes slightly a smaller amount of memory space than CFI-Stream. This is because CFI-Stream stores all closed itemsets in the DIU tree so that the frequent closed itemsets can be output based on any user-specified thresholds in real time. We can see that CFI-Stream is especially efficient for dense datasets in which the ratio between the number of frequent closed itemsets and the corresponding number of frequent itemsets is large.

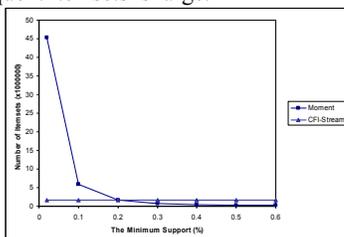


Figure 3. Memory usage (T10.I6.D100K)

5. CONCLUSIONS

In this paper we proposed a novel algorithm, CFI-Stream, to discover and maintain closed frequent itemsets in the current data stream sliding window. The algorithm offers an incremental method to check and maintain closed itemsets online. All closed frequent itemsets in data streams can be output in real time based on users' specified thresholds. Our performance studies show that this algorithm is able to mine data streams online with both time and space efficiency independent of support information, and it can adapt to the concept-drifting in data streams. Experimental results show that our method can achieve better performance than a representation algorithm for the state-of-the-art approaches in terms of both time and space overhead, especially when the minimum support is low, and the dataset is dense. In the future, we plan to extend our proposed algorithm to different data stream applications.

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